## POLITONG - SHANGHAI

## ELECTRONICS DEVICES -September 2012

NAME (Pinyin/Italian): $\qquad$

## MATRICULATION NUMBER:

$\qquad$

SIGNATURE: $\qquad$

NOTES:

- Use only these pages (including the back) for answers.
- Use of any book, note or other didactic material is not allowed. Only the use of simple calculator is allowed (notebooks or electronic tablets of any kind are not allowed).
- Write clearly and be explicit and concise in your answers. Include the basic formulas and logical steps used to reach the results. Provide the final numerical values.
- Questions in bold are considered more difficult.


## Exercise 1

a) Consider the resistor shown in Fig.1. Determine the value of the diameter $\boldsymbol{d}$ of the half circle of surface $\boldsymbol{S}$ to have a value of resistance $\mathbf{R}=\mathbf{1 0} \mathbf{k}$.
b) Given the current $\mathbf{I}=\mathbf{1 m A}$ flowing in the resistor, calculate the applied electric field $\boldsymbol{F}$.
c) Compensate now the semiconductor with acceptors. Calculate the concentration $\mathbf{N}_{\mathrm{A}}$ necessary to have still a $n$-type material with a concentration of majority carriers $10^{6}$ times larger than the concentration of minority carriers.


Figure 1

| Electron charge | $\mathrm{q}=1.6 \cdot 10^{-19} \mathrm{C}$ |
| :--- | :--- |
| Electron mobility | $\mu_{\mathrm{n}}=1400 \mathrm{~cm}^{2} / \mathrm{Vs}$ |
| Hole mobility | $\mu_{\mathrm{p}}=400 \mathrm{~cm}^{2} / \mathrm{Vs}$ |

d) Consider again the semiconductor with floating terminals (no current flowing) and with a gradient of doping between the two opposite surfaces (the ones where the terminals are applied) given by $N_{D 1}=10^{16} \mathrm{~cm}^{-3}$ and $\mathrm{N}_{\mathrm{D} 2}=5 \cdot 10^{16} \mathrm{~cm}^{-3}$. Determine the voltage difference in the semiconductor which is set between the two surfaces by the doping difference.

## Exercise 2

a) Consider the pn junction at equilibrium represented in Fig.2. Supposing $\mathbf{N}_{\mathrm{D}} \gg \mathbf{N}_{\mathrm{A}}$ and the width of the depletion layer $\mathbf{W}=\mathbf{1 1 0} \mathbf{n m}$, calculate the built-in voltage $\boldsymbol{\phi}_{i}$ and the doping $\mathbf{N}_{\mathrm{D}}$, justifying the approximation above.
b) Consider to bias the junction with a reverse voltage $\mathbf{V}_{\mathbf{R}}=10 \mathrm{~V}$. Calculate the maximum electric field $\boldsymbol{F}_{\text {MAX }}$ in the junction and the depletion capacitance (per unit of area) $\mathrm{C}_{\mathrm{j}}$. Justify used approximations.

Consider now the junction forward biased with $\mathbf{V}_{\mathbf{D}} \mathbf{= 0 . 6 5 V}$.
c) Determine if it is a short or long diode in the two regions.
d) Calculate the minority carriers concentration at the border of the neutral zone: $\mathbf{n}\left(-\mathbf{x}_{\mathrm{p}}\right)$ and $\mathbf{p}\left(\mathbf{x}_{\mathrm{n}}\right)$. Draw the minority carriers profile in the two regions.
e) Find the voltage $V_{D}$ at which the diffusion capacitance $C^{\prime}{ }_{d}$ is equal to the depletion capacitance $C_{j}^{\prime}$ (both per unit of area).

## Exercise 3

Consider the MOS junction shown in Fig.3a with parameters reported in Table 3.a.
a) Given a potential difference $\Delta \mathrm{V}_{\mathrm{SD}}=0.67 \mathrm{~V}$ in the silicon at threshold condition, calculate the doping concentration $\mathbf{N}_{\mathbf{A}}$.
b) Calculate the threshold voltage $\mathbf{V}_{\mathbf{T}}$.

Consider now the MOSFET shown in Fig.3b with parameters reported in Table 3.b and based on the same MOS structure considered at points $a$ ) and $b$ ).
c) Calculate the channel conductance $\mathbf{G}_{\mathrm{CH}}$ at the bias conditions: $\mathrm{V}_{\mathrm{SB}}=\mathbf{0}, \mathrm{V}_{\mathrm{GS}}=2.0 \mathrm{~V}, \mathrm{~V}_{\mathrm{DS}}=0.6 \mathrm{~V}$.
d) Given $\mathbf{V}_{\mathbf{S B}}=\mathbf{0}, \mathbf{V}_{\mathbf{G S}}=\mathbf{2 . 0} \mathbf{V}$ and $\mathbf{V}_{\mathrm{DS}}=\mathbf{2 . 0} \mathbf{V}$, determine the operation region of the MOSFET and calculate the transconductance $\boldsymbol{g}_{\boldsymbol{m}}$.
e) Operate the MOSFET at $\mathrm{V}_{\mathrm{SB}}=\mathbf{0}, \mathrm{V}_{\mathrm{GS}}=\mathbf{2} .0 \mathrm{~V}$ in ohmic region and determine $V_{D S}$ to have $50 \%$ of the transconductance of the point $d$ ).

| $]^{\text {G }}$ | Flat-band voltage $V_{F B}=-0.7 \mathrm{~V}$ $\mathrm{t}_{\mathrm{Ox}}=80 \mathrm{~nm}$ |
| :---: | :---: |
| Al |  |
| Oxide $\hat{l}^{\text {tox }}$ |  |
| $\underset{\substack{\text { silicon } \\ N_{A}}}{ }$ | Table 3.a |
| AI |  |
| , в <br> Figure 3.a |  |
| - G | $\begin{aligned} & \mathrm{L}=10 \mu \mathrm{~m} \\ & \mathrm{~W}=100 \mu \mathrm{~m} \\ & \mu_{\mathrm{n}}=1400 \mathrm{~cm}^{2} / \mathrm{Vs} \end{aligned}$ |
| So Al |  |
|  |  |
|  |  |
| ${ }_{\text {Al }}$ |  |
| - ${ }^{\text {}}$ |  |
| Figure 3.b | Table 3.b |
| Intrinsic concentration | $\begin{aligned} & \mathrm{n}_{\mathrm{i}}=1.45 \cdot 10^{10} \mathrm{~cm}^{-3} \\ & \varepsilon_{0}=8.85 \cdot 10^{-14} \mathrm{~F} / \mathrm{cm} \end{aligned}$ |
| Dielectric constant in vacuum |  |
| Relative dielectric contant in Si | $\varepsilon_{\mathrm{r}-\mathrm{Si}}=11.7$ |
| Dielectric constant in Si | $\begin{aligned} & \varepsilon_{\mathrm{Si}}=\varepsilon_{0} \cdot \varepsilon_{\mathrm{r}-\mathrm{Si}} \approx 1 \mathrm{pF} / \mathrm{cm} \\ & \mathrm{k}=1.38 \cdot 10^{-23} \mathrm{~J} / \mathrm{K} \end{aligned}$ |
| Boltzmann constant |  |
| Thermal voltage | $\mathrm{V}_{\mathrm{TH}}=25 \mathrm{mV}$ |
| Electron charge | $\mathrm{q}=1.6 \cdot 10^{-19} \mathrm{C}$ |
| Dielectric constant in Oxide | $\varepsilon_{O x}=\varepsilon_{0} \varepsilon_{r-O x} \approx 1 / 3 \mathrm{pF} / \mathrm{cm}$ |

## Theory question \#1:

Demonstrate the formula of the drift current in a semiconductor. Ohm law, conducibility, resistance, dependence from dopant concentration. Why in semiconductors there is a bipolar current? Give its expression.

## Theory question \#2:

MOSFET transistor: discuss the change current with the drain voltage in relation to a change of the pinch-off point. What it is introduced in the transistor model to take into account of this phenomenon?

